

30 **Abstract**

31 Biomechanical motion data involving impacts are not adequately represented using
32 conventional low-pass filters (CF). Time-frequency filters (TFF) are a viable alternative, but
33 have been largely overlooked by movement scientists. We modified Georgakis and
34 Subramaniam's (2009) fractional Fourier filter (MFrFF) and demonstrated it performed better
35 than CFs for obtaining lower leg accelerations during football instep kicking. The MFrFF
36 displayed peak marker accelerations comparable to a reference accelerometer during foot-to-
37 ball impact (peak % error = $-5.0 \pm 11.4\%$), whereas CFs severely underestimated these peaks
38 (30 - 70% error). During the non-impact phases, the MFrFF performed comparably to CFs
39 using an appropriate (12 - 20Hz) cut-off frequency (RMSE = $37.3 \pm 7.6 \text{ m/s}^2$ vs. 42.1 ± 11.4
40 m/s^2 , respectively). Since accuracy of segmental kinematics is fundamental for understanding
41 human movement, the MFrFF should be applied to a range of biomechanical impact scenarios
42 (e.g. locomotion, landing and striking motions) to enhance the efficacy of study in these areas.

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54 **Introduction**

55 Accurate quantification of velocities and accelerations using camera-based motion analysis is
56 essential for understanding human movement. To minimise high frequency error from soft
57 tissue artefact and system limitations, marker displacements are low-pass filtered prior to
58 calculation of such parameters (Giakas et al., 2000; Robertson and Dowling, 2003). However,
59 conventional low-pass filters (CFs) (e.g. digital filters) have been criticised for their inability to
60 treat motions involving impacts (Giakas et al., 2000). Since impacts amplify the frequency
61 content of the motion of the impacting body (i.e. causes sudden deceleration) (Georgakis et
62 al., 2002a,b), yet CFs use a constant cut-off frequency for the entire signal time-series (Figure
63 1), they cannot optimally remove high frequency error from impact and non-impact phases
64 concurrently. This may lead to distortion of variables near to impact and erroneous
65 interpretation of the movement in question (Knudson and Bahamonde, 2001; Nunome et al.,
66 2006). For example, lower limb kinematics have been used to predict injury during foot-to-
67 ground contact in locomotion (Milner et al., 2006; Pohl et al., 2008) and landing motions
68 (Hewett et al., 2005), and distal endpoint kinematics as performance indicators in striking
69 sports (Joyce et al., 2011; Marshall and Elliott, 2000). Use of CFs may ultimately restrict our
70 ability to understand injury risk or performance in these scenarios.

71 One alternative is to use a filter with a time-varying cut-off frequency, or time-frequency filter
72 (TFF) (Giakas et al., 2000). When the impact induces expansion of the frequency content of
73 a marker, the TFF increases the cut-off value so signal to noise ratios are optimised. TFFs
74 have been used extensively in optics, speech and music processing, and biomedical
75 engineering (Ozaktas et al., 1996), but have been largely ignored by biomechanists. This is
76 despite evidence TFFs outperform CFs during aforementioned activities (e.g. running, Alonso
77 et al., 2005; landing, Georgakis et al., 2002a; and ball kicking, Nunome et al., 2006). Georgakis
78 and Subramaniam's (2009) fractional Fourier filter (FrFF) is one TFF that has been designed
79 for use with marker displacement data, but has not been widely implemented. The FrFF
80 processes marker trajectories in consecutive fractional Fourier domains, and the current study

81 modified the algorithm (MFrFF) (i.e. filter parameter selection) for use during ball kicking
82 motions. Since accurate determination of lower leg kinematics is key for understanding ball
83 kicking performance (Nunome et al., 2006), the aim of this study was therefore to determine if
84 the MFrFF performed better than CF methods for obtaining lower leg accelerations during
85 impact and non-impact phases of football instep kicking.

86 **Methods**

87 **Fractional Fourier Filter Parameter Selection and Implementation**

88 Georgakis and Subramaniam (2009) described the design and operation of the FrFF. The
89 algorithm uses a 'triangular' filter boundary which raises the cut-off frequency to retain the
90 time-dependent expansions in frequency content during an impact and determines the
91 appropriate fractional domains with cut-off values based on triangular boundary parameters
92 (Figure 1).

93 ****Figure 1 near here****

94 Filter boundary parameters were determined as follows. Non-impact phase cut-off frequencies
95 (X_1), were determined by residual analysis (Winter, 2009). The time of maximum acceleration
96 during impact (t_I) was determined as the instance of peak acceleration (2nd derivative of
97 unfiltered marker displacement) ± 10 ms of the temporal midpoint of impact. Impact width
98 (W) and height (H) were optimised by selecting the filter solution that minimised: a) absolute
99 error (m/s^2) between peak accelerations obtained from MFrFF filtered and unfiltered marker
100 trajectories (i.e. maintaining peak acceleration during impact) and b) mean square error
101 between accelerations from the MFrFF and CF filtered marker trajectory (4th order, dual pass,
102 Butterworth filter, 18 Hz cut-off) $\pm 10 - 50$ ms either side of impact (i.e. reducing high frequency
103 content during pre and post non-impact phases). Iterative implementation of the MFrFF using
104 the '*fminsearch*' optimisation function within Matlab (2017a, Natick, USA) determined the
105 magnitudes of, and ratio between W and H that best satisfied a) and b) for a given marker
106 trajectory. The starting point for calculations was a W to H ratio of 1:11000 (if $W = 0.01s$, $H =$

107 110 Hz) and initial W was manually determined by acceleration of the ball above and below
108 200 m/s^2 (i.e. ball contact start and end; Nunome et al., 2006). Custom Matlab scripts
109 implemented these routines on individual marker trajectories (i.e. separate X, Y and Z
110 components).

111 **Experiment, Data Collection and Analysis**

112 Football instep kicking induces a considerable impact as the foot contacts the ball (Nunome
113 et al., 2006). If a CF is used to filter 'through' the impact phase, kinematic variables near the
114 time of impact will contain considerable error (Knudson and Bahamonde, 2001). Thus,
115 accelerations from marker trajectories filtered by each MFrFF and five variations of a CF were
116 compared to those from a reference accelerometer (1000 Hz, 14 x 13 x 14 mm, 8 g; ± 1000
117 G; S3-1000GHA, Biometrics Ltd, Newport, UK). CFs were variations of a 4th order, dual pass,
118 zero lag Butterworth digital filter (chosen as the most commonly used methods in ball kicking
119 literature; Table 1).

120 **Table 1 near here**

121 Following institutional ethical approval and written informed consent, eight semi-professional
122 male footballers ($77.3 \pm 4.1 \text{ kg}$, $1.78 \pm 0.05 \text{ m}$, $25.8 \pm 2.9 \text{ years}$) performed ten maximal kicks
123 with a size 5 ball. The accelerometer was attached to the lateral side of the kicking leg 5 cm
124 above the malleolus on a line towards the femoral epicondyle, and tape was wrapped around
125 the leg to ensure it was stationary relative to the shank. Accelerations were filtered on-board
126 by an elliptical filter (cut-off = 312 Hz). The synchronised motion of a reflective marker (12.6
127 mm) placed on the accelerometer was recorded by a 10-camera, motion analysis system
128 (1000Hz; Vicon T40S, Vicon Motion Systems, Oxford, UK). Trajectories were exported to
129 Visual 3D (V6, Rockville, USA), replicated and filtered in the six filter conditions. Dependent
130 variables were root mean square error (between initiation of final stride to end of follow
131 through; RMSE) and percent peak error during impact (%PE) of resultant accelerations

132 (magnitude of X, Y, Z components) between the accelerometer and motion analysis data (2nd
133 derivative of marker trajectory calculated by finite differences).

134 One-way repeated measures ANOVAs determined differences in RMSE and %PE between
135 the six filter conditions, compared to accelerometer. If sphericity was violated (Mauchly's = P
136 < 0.05), the Greenhouse-Geisser adjustment was used. Alpha for main effects was Bonferroni
137 adjusted to $\alpha = 0.025$. Bonferroni adjusted contrasts determined pairwise differences between
138 each CF and the MFrFF to further control Type-I error ($\alpha = 0.005$). Effect sizes were calculated
139 as per Cohen (1988). The 95% limits of agreement (LOA; Bland and Altman, 1999) between
140 accelerometer and motion analysis were also calculated for peak values at impact (N = 80
141 trials). All statistical tests were conducted using SPSS (V23, IBM, New York, USA).

142 **Results**

143 Both RMSE and %PE were different between filter conditions ($p < 0.001$). The MFrFF
144 produced smaller %PE ($-5.0 \pm 11.4\%$) compared to the reference accelerometer than each
145 CF ($p < 0.001$; Table 2), with large effect sizes ($d > 0.8$). The BW-250 and BW-DS ($228.8 \pm$
146 75.4 and 49.1 ± 7.9 m/s², respectively) produced larger RMSE values than MFrFF ($p < 0.001$;
147 Table 2), whereas BW-REF (25.4 ± 10.8 m/s²) produced smaller RMSE values than MFrFF
148 (37.3 ± 7.6 m/s²; $p < 0.001$). Effect sizes were moderate to large ($d > 0.5$ or $d > 0.8$).

149 In absolute terms, the MFrFF produced peak accelerations that were 41.6 m/s² larger than the
150 accelerometer, but might produce accelerations 133.2 m/s² less than (95% CI = 108.3 – 158
151 m/s²) or 233.3 m/s² greater than (95% CI = 208.2 – 258.2 m/s²) the accelerometer (Table 2).
152 The BW-12, BW-20, BW-REF and BW-DS displayed 95% LOA that were exclusively lower
153 than the accelerometer (upper limits ratio < 1) and the BW-250 displayed excessively wide
154 LOA. A representative comparison of time-series accelerations obtained from each filter
155 condition is shown in Figure 2.

156 **Table 2 and Figure 2 near here**

158 **Discussion**

159 **Filter Performance**

160 The MFrFF accurately detected rapid decelerations at the lower leg during foot-to-ball contact,
161 whereas CFs could not. The MFrFF thus retained most high frequency marker content owing
162 to physical sources, while the majority of high frequency noise was attenuated. This supports
163 research that used TFFs to accurately represent landing (Georgakis and Subramaniam, 2009)
164 and ball kicking impact kinematics (Nunome et al., 2006). The BW-250 also retained high-
165 frequency content during impact, but these values were likely indicative of noise that was
166 evident throughout the kick (Figure 2). Conversely, CFs that filtered through impact using a
167 low-cut off frequency severely underestimated marker accelerations during impact. All high
168 frequency content was removed and the sudden deceleration owing to impact was not evident.
169 BW-12 and BW-DS also showed decelerations occurring before impact, which is known to be
170 a result of over filtering (Knudson and Bahamonde, 2001; Nunome et al., 2006). Finally, the
171 BW-REF accurately produced marker accelerations up until ball impact, but was unable to
172 detect changes during and after the impact (Knudson and Bahamonde, 2001). This condition
173 also produced significantly lower RMSE values than the MFrFF, but this was due to the error
174 introduced during and post impact that was included for the MFrFF and missing for the BW-
175 REF.

176 As well as performing better during impact, the MFrFF also adequately removed high
177 frequency noise from the pre and post impact swing phases. RMSE values were comparable
178 to CFs that used a high sampling rate (1000Hz) and low cut-off frequency (i.e. BW-12 and
179 BW-20) and these methods are known to produce valid accelerations during motions without
180 an impact (Giakas et al., 2000; Robertson and Dowling, 2003). Furthermore, the BW-250
181 condition was unable to adequately attenuate high-frequency noise during the non-impact
182 phase, and displayed inadequately large RMSE values. Ultimately, the MFrFF maintained
183 good signal to noise ratios during both impact and non-impact phases of the kick, whereas
184 CFs could not.

185 **Practical Implications**

186 The current study modified the FrFF (Georgakis and Subramaniam, 2009) to accurately
187 quantify kinematics during football instep kicking (Nunome et al., 2006). The MFrFF could thus
188 be used to enhance the efficacy of future study involving ball kicking. Furthermore, while this
189 is only one example of MFrFF application, the method has potential to enhance understanding
190 of other human motion involving impacts (e.g. landing and running motions). Since CFs may
191 result in flawed velocities and accelerations near to impact (Knudson and Bahamonde, 2001),
192 researchers should carefully consider the effect that filter choice has on practical interpretation
193 of their data. Interactions occur between the body and the external environment in almost all
194 examples of human motion, and these invariably induce marker displacements that
195 necessitate use of a TFF. It is therefore important TFF methods become widely implemented,
196 and future research should assess the efficacy of TFFs for quantifying kinematic variables
197 during other human movement scenarios.

198 The MFrFF also addressed some of the barriers that have prevented widespread application
199 of TFFs. First, MFrFF parameter selection was almost entirely automated. The only user input
200 required was to determine the temporal start and end of the impact (Alonso et al., 2005). The
201 chances of manually selecting erroneous parameters and obtaining a non-optimal filter
202 solution were thus minimised. Second, the optimisation process selected filter parameters
203 exclusively from the physical characteristics of marker displacements. While this is not
204 necessarily a novel feature of the FrFF, this study showed the original method can be readily
205 adapted for different impact scenarios. Third, while it is acknowledged the MFrFF required
206 higher sampling rates than commonly used in ball kicking studies (~100 - 500 Hz; Kellis and
207 Katis, 2007), this is typically possible in most well-equipped laboratories. Higher sampling
208 rates are necessary to ensure enough data points are included during the short duration of
209 impact (~10 ms) to allow the FrFF to function correctly. Finally, to date, only the theoretical
210 and computational details of TFFs are available (Georgakis et al., 2002a,b; Georgakis and
211 Subramaniam, 2009). Since these are often complex, it is difficult for researchers to use TFFs

212 without designing their own parameter selection and implementation algorithms. To be useful,
213 future research should present TFFs in formats that are readily integrated with software tools
214 commonly used by motion scientists.

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217 **Conflicts of interest statement**

218 The authors declare no competing, or financial interests.

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281 **Tables**

282 Table 1. Description of conventional filter conditions. Filter cut-offs of ‘filtered through’
 283 conditions were chosen to represent studies that have focussed on swing phase (BW-12 and
 284 BW-20; e.g. Dorge et al., 2002) or ball impact kinematics (BW-250; e.g. Shinkai et al., 2009).
 285 The BW-REF was chosen to show the influence of truncating data before the onset of impact
 286 (e.g. Ball, 2008) and BW-DS the effect of down sampling data to a rate comparable to the
 287 majority of ball kicking literature (~100 - 400Hz; Kellis and Katis, 2007).

Filter Name	Filter Type	Sample Rate (Hz)	Cut-Off Frequency (Hz)	Impact Phase	Start and End Endpoint Extrapolation
BW-12	4th order, dual pass Butterworth	1000	12	Filtered through	One-hundred frames reflection, removed following filter application
BW-20	4th order, dual pass Butterworth	1000	20	Filtered through	One-hundred frames reflection, removed following filter application
BW-250	4th order, dual pass Butterworth	1000	250	Filtered through	One-hundred frames reflection, removed following filter application
BW-REF	4th order, dual pass Butterworth	1000	20	Truncated one frame before ball contact initiated	One-hundred frames reflection, removed following filter application
BW-DS	4th order, dual pass Butterworth	250	12	Filtered through	Twenty-five frames reflection, removed following filter application

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302 Table 2. Mean \pm s.d. percent peak error (%PE) and root mean square error (RMSE) values of
 303 each filter condition compared to accelerometer data, pairwise comparisons of each
 304 conventional filter technique with the MFrFF, and ratio 95% limits of agreement between peak
 305 resultant accelerations obtained at ball impact from each filter condition and the reference
 306 accelerometer (N = 80 trials).

		MFrFF	BW-12	BW-20	BW-250	BW-REF	BW-DS
%PE (%)	Mean \pm s.d.	-5.0 \pm 11.4	66.7 \pm 7.1	54.1 \pm 9.1	-25.4 \pm 18.3	36.1 \pm 24.2	64.9 \pm 10.7
	p-value		<0.001*	<0.001*	<0.001*	0.001*	<0.001*
	Effect size (d)		7.6	5.7	-1.3	2.2	6.5
RMSE (m/s ²)	Mean \pm s.d.	37.3 \pm 7.6	45.4 \pm 10.8	42.1 \pm 11.4	228.8 \pm 75.4	25.4 \pm 10.8	49.1 \pm 7.9
	p-value		0.023	0.152	<0.001*	0.001*	<0.001*
	Effect size (d)		0.8	0.4	3.6	-1.3	1.5
		Ratio differences with accelerometer		Ratio 95% limits of agreement with accelerometer			
		Mean	SD	Lower Limit	[95% CI]	Upper Limit	[95% CI]
	MFrFF	1.05	0.11	0.84	[0.81-0.87]	1.28	[1.25-1.31]
	BW-12	0.33	0.24	0.22	[0.16-0.27]	0.50	[0.45-0.55]
	BW-20	0.46	0.15	0.37	[0.33-0.40]	0.63	[0.60-0.67]
	BW-250	1.26	0.25	0.75	[0.70-0.81]	1.78	[1.72-1.84]
	BW-REF	0.64	0.19	0.42	[0.38-0.46]	0.81	[0.77-0.85]
	BW-DS	0.33	0.24	0.21	[0.16-0.27]	0.50	[0.44-0.55]

* denotes significantly different to FrFF condition (P < 0.005).

d = 0 - 0.2 trivial effect, 0.2 - 0.5 small effect, 0.5 - 0.8 = medium effect, > 0.8 large effect.

Positive values show peak value from accelerometer was greater than from motion analysis, and vice versa.

Ratio > 1.00 indicates that motion analysis gave a higher acceleration than the accelerometer.

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315 **Figure Captions**

316 Figure 1. Example showing constant cut-off frequency (f_c) of conventional filter (left) and time-
317 varying f_c boundary of the fractional Fourier domain filter (right). X_1 = cut-off of non-impact
318 phase, W = width of impact, H = height of impact, t_i = time of impact centre.

319 Figure 2. Representative trial showing time-series resultant accelerations (magnitude of X, Y
320 and Z components) obtained from accelerometer (red line) and the six filter conditions (black
321 lines) between the events of initiation of final stride (0.6 s) and end of follow through (0.7 s).
322 The respective filter condition is shown above each plot. Vertical dashed lines indicate the
323 start and end of ball impact, respectively.

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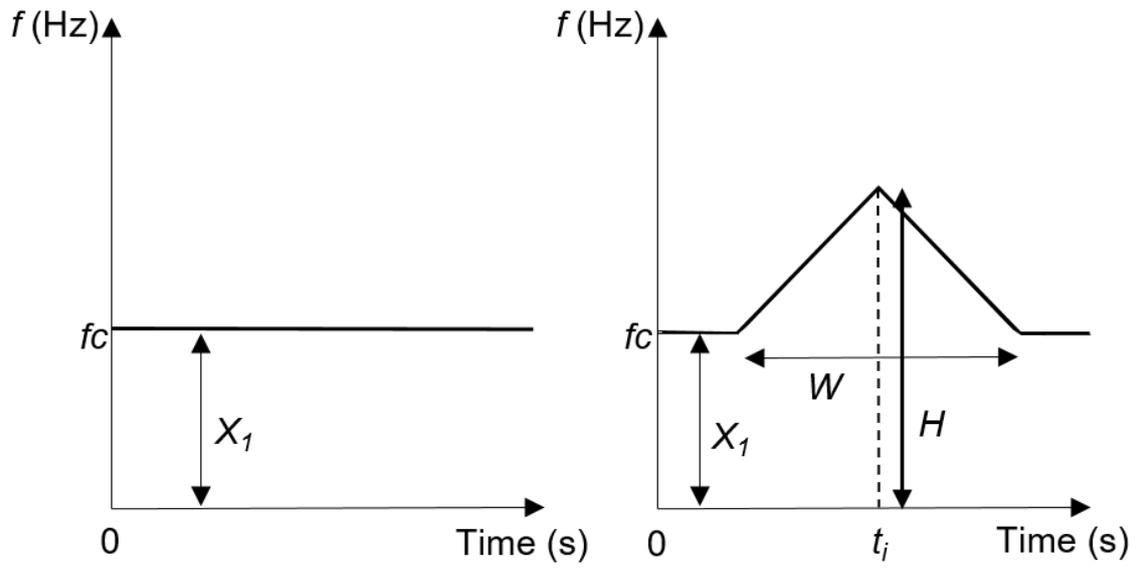
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343 Figure 1.



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